

Group 1:

- 1) A license plate has **four letters** followed by **two numbers**. How many different license plates can be made?
- 2) How many different outfits can be made from **3** pairs of shoes, **4** shirts, and **2** pairs of jeans?
- 3) Two **6**-sided die are rolled. How many possible outcomes are there?

Group 2:

- 1) A license plate has **three letters** followed by **three numbers**. How many different license plates can be made?
- 2) How many different meals can be made from **2** appetizers, **5** entrees, and **3** desserts?
- 3) A **4**-sided die, and a **6** sided die are rolled. How many possible outcomes are there?

#learning

Today we will determine how many outcomes are possible when considering order and position.

Keys:

- I can determine if a situation is an arrangement, permutation or combination.
- I can calculate the number of possible outcomes

World 9-2

ARRANGEMENTS, COMBINATIONS, AND
PERMUTATIONS

Arrangements

- Definition: An arrangement is the act of ordering SOME of the items in a set.
- 6 swimmers are competing for the gold, silver, and bronze medals. How many possible ways are there to give out the medals?

$$\begin{aligned} \text{Total \#} &= \text{\# of people to} && \text{\# of people to} && \text{\# of people to} \\ \text{of ways} &= \text{get Gold} && \text{get Silver} && \text{get Bronze} \\ & && \times && \times \\ &= 6 \times 5 \times 4 = 120 \text{ possibilities!} \end{aligned}$$

- Can I have 3 volunteers?
- How many ways can we organize this four fine folks in a line?
- Answer....
- 6 ways! (3 x 2 x 1)

PERMUTATIONS



How many ways can we arrange x number of cars in their parking spots.

x=3 cars (R, Y, B)

RYB
RBY
YBR = 6 different options
YRB
BYR
BRY

Or,
 $3 \times 2 \times 1 = 6$

x=4 cars (R, Y, B, W)

$$\boxed{4} \times \boxed{3} \times \boxed{2} \times \boxed{1} = 24$$

X=5 cars (R, Y, B, W)

= 120 ways

More specifically a **Permutation** is an ordered arrangement of ALL items in a set.

To Remember: **P**ermutation think **P**osition

eg. 1 Organizing 3 students in a row

3 2 1 $3 \times 2 \times 1 = 3!$ or 6 permutations

eg. 2 Organizing 6 books on a shelf.

6 5 4 3 2 1

$6 \times 5 \times 4 \times 3 \times 2 \times 1 = 6!$ Or 720 permutations

If order doesn't matter, you have a COMBINATION.



They should really call it a “Permutation Lock”

A **Combination** is choosing some items from a set of n elements.

The order does not matter.

Remember: **Combination think Choose**

Ex 4: Three friends out of a group of five have to go help Mrs. Cameron carry books to the library. How many combinations of friends can be picked?

$$\begin{array}{l} \text{Number of} \\ \text{combinations} \end{array} = \frac{\boxed{\# \text{ of Arrangements of the 3 friends}}}{\boxed{\text{Permutation of} \\ \text{the 3 friends}}}$$

$$\begin{array}{l} \text{Number of} \\ \text{combinations} \end{array} = \frac{5 \times 4 \times 3}{3!} = \frac{60}{6} = 10 \text{ combinations}$$

eg. 2 Pick 4 Pool balls out of 16 to place on the table.



$$\# \text{ of Combinations} = \frac{\# \text{ of arrangements for the 4 balls}}{\# \text{ of permutations for the 4 items}}$$

$$\# \text{ of Combinations} = \frac{(\text{ways to pick \#1}) \times (\text{ways to pick \#2}) \times (\text{ways to pick \#3}) \times (\text{ways to pick \#4})}{\# \text{ of permutations for the 4 items}}$$

$$\# \text{ of Combinations} = \frac{16 \times 15 \times 14 \times 13}{4!} = 1820$$

Therefore one can pick 1820 different combinations of 4 pool balls from 16 on the table.

Permutations vs Combinations

Challenge



Permutation or Combination

A) One chooses 3 different toppings on a tofu burger from a choice of 15 toppings.

Combination

~~Permutation~~



Permutation or Combination

B) Arrange all 6 shirts in your closet. Order is important.

~~Combination~~

Permutation



Permutation or Combination

C) Take your two favourite movies from a collection of 15 dvds to a friend's for a slumber party.

Combination

~~Permutation~~



Permutation or Combination

D) Make a poker hand by taking the top 5 cards from a deck.

Combination

~~Permutation~~



Permutation or Combination

E) A teacher organizes all 12 class tests in alphabetical order.

~~Combination~~

Permutation



SUMMARY

